Reconfigurable Wideband Ground Receiver Hardware Description and Laboratory Performance

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Recently, much effort has been placed toward the development of the Reconfigurable Wideband Ground Receiver (RWGR): a variable-rate, reprogrammable software-defined radio intended to supplement and augment the capabilities of the Block V Receiver. In this report, we first give an overview of the hardware architecture of the RWGR, including a detailed description of the filter-decimate front-end and subsequent high-rate receiver system, which includes a 4 sample/symbol demodulator core. We then present a series of laboratory hardware performance results, including bit error rate (BER) results at various data rates. The RWGR is shown to yield performance close to theory in terms of BER with losses typically less than 1 dB in bit signal-to-noise ratio (SNR).

I. Introduction

To address the future telemetry, navigation, and radio science needs of the Deep Space Network (DSN), considerable effort at JPL has been directed toward the development of a wideband ground receiver, intended to supplement and expand the capabilities of the currently operational Block V Receiver (BVR). Among the challenges encountered in this effort has been the need to process both high data rate telemetry (well in excess of 150 Mbps), as well as telemetry from very low-rate missions. Another key element of this work has been the selection of a processing platform that is well-suited to firmware and software reconfigurability. These objectives have led to the development of the Reconfigurable Wideband Ground Receiver (RWGR): a variable data rate,

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reprogrammable *software-defined radio*. The RWGR is an intermediate frequency (IF) sampling receiver that operates at a fixed input sampling rate of 1.28 GHz. It is designed to accommodate a continuous range of data rates from 4 Bd (symbols/second or baud) to 320 MBd, and is capable of processing 500 MHz of bandwidth. In contrast, the BVR operates at a sample rate of 160 MHz and can only accommodate a bandwidth of 72 MHz.

The actual hardware for the RWGR is directly based upon a processing platform from a family of ground-based instruments fielded within the DSN for radio science and navigation applications. These include variants of the Radio Science Receiver (RSR)¹ and Wideband VLBI Science Receiver (WVSR)² [1]. It was envisioned that the process of demonstration and infusion would be simplified through the selection of a common hardware base for developing enhanced telemetry processing capabilities.

To facilitate the accommodation of such a wide range of data rates, the RWGR processes wideband and narrowband waveforms differently. Higher rate wideband signals are processed using field programmable gate array (FPGA)-based hardware, whereas lower rate narrowband signals are processed in software using downconverted sampled data obtained from the hardware. Specifically, the hardware receiver is used to accommodate higher data rates in the range of 39.0625 kBd to 320 MBd (suppressed carrier), while the software demodulator is used to process lower data rates in the range of 4 Bd to 1 MBd (suppressed carrier, residual carrier, and subcarrier modulation types). In either case, continuous data rate support is accomplished through two mechanisms: a coarse decimation filtering stage to lower the bulk of the data rate followed by a fine interpolation stage to further lower the data rate to the exact desired value.

In this report, we focus on the hardware aspects of the RWGR. First, we present an overview of the hardware architecture, including a detailed implementation description of the filter-decimate front-end and subsequent high-rate receiver system which includes a 4 sample/symbol demodulator core. Then, we present a series of laboratory performance results for the hardware receiver. Hardware soft symbol output density plots are shown for a variety of data constellations, including quadrature phase shift keying (QPSK) [2] and 16-ary quadrature amplitude modulation (QAM) (i.e., 16-QAM) [2]. In addition, bit error rate (BER) results are provided for various data rates and modulation types, including offset QPSK (OQPSK), and compared with ideal results from theory. As we show, the RWGR yields performance close to theory in terms of uncoded BER with losses typically less than 1 dB in bit signal-to-noise ratio (SNR).

A. Outline

A detailed overview of the hardware architecture implementation is provided in Section II. Specifically, the filter-decimate front-end is detailed in Section II.A, including a discussion

¹http://psdg.jpl.nasa.gov/wiki/Radio_Science_Receivers (internal JPL website)

²http://psdg.jpl.nasa.gov/wiki/WVSR_Phase_II (internal JPL website)

on the open-loop predict-driven Doppler frequency compensation in Section II.A.1 and the reprogrammable decimation filter coefficients in Section II.A.2. In Section II.B, we focus on the subsequent high-rate receiver core, highlighting the fine interpolator system in Section II.B.1 and various aspects of the 4 sample/symbol demodulator core in Section II.B.2. Laboratory hardware results are presented in Section III. Noiseless soft decision density plots are shown in Section III.A for a variety of modulation types. In addition, several BER results are provided in Section III.B and compared with theory, including high data rate results in Section III.B.1, variable data rate results in Section III.B.2, and Gaussian minimum shift keying (GMSK) [3] demodulation results in Section III.B.3. Finally concluding remarks are made in Section IV.

B. Notations

All notations used are as in [4] and [5]. In particular, parentheses and square brackets are used to denote continuous-time (analog) and discrete-time (digital) function arguments, respectively. For example, x(t) would denote a continuous-time analog signal for $t \in \mathbb{R}$, whereas y[n] would denote a discrete-time digital signal for $n \in \mathbb{Z}$. In addition to this, analog frequencies and digital normalized frequencies will be respectively denoted by Fand f. Hence, $X(j2\pi F)$ would denote the continuous-time Fourier transform of x(t) where F is in units of Hz, while $Y(e^{j2\pi f})$ would denote the discrete-time Fourier transform of y[n] where f is normalized to the sampling frequency F_s (i.e., $f = \frac{F}{F_s}$).

II. Detailed Description of Hardware Architecture

A block diagram of the overall RWGR hardware system is shown in Figure 1. The underlying analog telemetry signal received is first downconverted from radio frequency (RF) to intermediate frequency (IF) [2]. Afterward, the resulting analog IF signal is then sampled by an 8-bit analog-to-digital converter (ADC) operating at a fixed sample rate of $F_s = 1.28$ GHz. The stream of 8-bit ADC IF samples is then sent to an input FPGA which then sends the data to either the filter-decimate FPGA or the high-rate receiver core FPGA, depending upon the data rate of the telemetry waveform. Specifically, samples corresponding to lower data rate signals (39.0625 kBd to 40 MBd) are sent to the filter-decimate FPGA for coarse downsampling prior to demodulation, whereas higher data rate signals (40 MBd to 320 MBd) are sent directly to the high-rate receiver core for finer downsampling followed by demodulation. The reason for this is that the filter-decimate FPGA performs a minimum decimation by a factor of 8:1. As such, higher data rate waveforms which require a decimation factor of D:1 for $1 \leq D < 8$ must bypass the filter-decimate FPGA altogether and be sent directly to the high-rate receiver core FPGA.

Interface to the software demodulator is provided through the receiver core FPGA. Specifically, the hardware system will simply perform a combination of coarse/fine decimation of a lower rate telemetry signal prior to passing the resulting downsampled data stream to the software demodulator for further processing.



Figure 1. Overall RWGR hardware system block diagram.

A. Filter-Decimate Front-End

A block diagram of the RWGR filter-decimate FPGA which highlights implementation details is shown in Figure 2. As can be seen, the filter-decimate system first demultiplexes the data into 8 parallel streams operating at a clock rate of 160 MHz (i.e., (1.28 GHz)/8). Since the outputs of the filter-decimate system can only be processed and transferred at a maximum rate corresponding to this clock rate, the result is a minimum decimation of the input data by a factor of 8 : 1. Data at the output here is transferred to the high-rate receiver core FPGA via a RocketIO interface.

The filter-decimate system contains two distinctive features which separate it from



Figure 2. RWGR filter-decimate FPGA implementation block diagram.

conventional coarse decimation filter systems: an open-loop predict-driven numerically controlled oscillator (NCO) for Doppler compensation and reprogrammable decimation filters. These are described below as follows.

1. Open-Loop Predict-Driven Doppler Compensation

From Figure 2, it can be seen that the filter-decimate FPGA accepts Doppler frequency predict files. These files consist of the predicted values of the Doppler frequency at 1 pulse-per-second (pps) epochs corresponding to Coordinate Universal Time (UTC) time tags. Along with a given frequency predict file, a 1 pps epoch UTC time tag input to the filter-decimate FPGA is used to generate open-loop predicts of the Doppler frequency at a 1 Hz update rate. The UTC 1 pps time tag is also converted to a Network Time Protocol (NTP) time-code which can then be sent out along with the decimated data for internal precision time tagging.

Here, the open-loop NCO (baseband mixer) from Figure 2 consists of a 40-bit phase accumulator which allows for phase continuous tuning. This corresponds to a frequency resolution of $(1.28 \text{ GHz})/2^{40} = 1.16 \text{ mHz} < 5 \text{ mHz}$. Thus, the filter-decimate system provides open-loop predict-driven Doppler frequency compensation at a resolution finer than 5 mHz at an update rate of 1 Hz.

2. Reprogrammable Decimation Filters

As can be seen from Figure 2, the filter-decimate FPGA performs power-of-two decimation from 8 : 1 to 1,024 : 1 (i.e., 2^{ℓ} : 1 for $3 \leq \ell \leq 10$). Specifically, a coarse decimation factor of 2^k is input to the system as well as the coefficients of the corresponding decimation filter $H_k(z)$. The coefficients of the decimation filter $H_k(z)$ are fully reprogrammable and are easily modifiable to accommodate a variety of applications. By default, $H_k(z)$ is given in terms of a *nominal* decimation filter $\overline{H}_k(z)$, whose magnitude response is shown in Figure 3. Here, the nominal decimation filter $\overline{H}_k(z)$ is a linear phase finite impulse response (FIR) filter [4] designed using the following criteria.

- The number of coefficients used was 2^{k+3} .
- The peak-to-peak passband ripple [4] (i.e., $20 \log_{10} \left(\frac{1+\delta_P}{1-\delta_P}\right)$) was chosen to be 0.1 dB.
- The stopband attenuation [4] (i.e., $-20 \log_{10} \delta_S$) was chosen to be 50 dB.
- The -6 dB cut-off frequency [4] f_c was chosen to be at the decimated Nyquist frequency [5] of $\frac{1}{2^{k+1}}$.

By default, the k-th decimation filter $H_k(z)$ is given in terms of the nominal filter $\overline{H}_k(z)$ as follows:

$$H_k(z) = G_0 \overline{H}_k(z) \quad \forall \ 3 \le k \le 10 \tag{1}$$



Figure 3. Magnitude response of the 2^k : 1 nominal decimation filter $\overline{H}_k(z)$ of the filter-decimate system ($3 \le k \le 10$).

Here, G_0 is a gain factor common to all decimation factors. The relation given in Equation (1) is appropriate for situations in which the input signal power level is constant as a function of the data rate. This, however, is not a realistic assumption in practice. Typically, the input signal power will be proportional to the data rate. In order to ensure that the signal level at the output of the decimation filter system is the same for all data rates, an additional gain factor of $2^{\frac{k}{2}}$ must be applied to the nominal filter $\overline{H}_k(z)$ to obtain the proper decimation filter $H_k(z)$. In other words, in practice, the k-th decimation filter $H_k(z)$ should be set in terms of the nominal filter $\overline{H}_k(z)$ as follows:

$$H_k(z) = 2^{\frac{k-3}{2}} G_1 \overline{H}_k(z) \quad \forall \ 3 \le k \le 10 \tag{2}$$

Here, G_1 is the gain factor for the first decimation filter $H_3(z)$ corresponding to a decimation of 8 : 1.

Another way to show why Equation (2) represents an appropriate scaling rule in practice is to consider the underlying physical layer of the telemetry waveform. In practice, the ambient white noise power spectral density (psd) [2] level N_0 will be constant for all possible data rates. To ensure an acceptable bit SNR E_b/N_0 for all data rates, where E_b denotes the signal energy per bit [2], it follows that E_b must be held constant as well. However, E_b is given by $E_b = \frac{P_s}{\mathcal{R}_b}$, where P_s denotes the signal power and \mathcal{R}_b denotes the bit rate. For weaker telemetry signals, P_s will be lower and so the only way for E_b to remain constant is for \mathcal{R}_b to decrease proportionally to P_s . This is typically what is done in practice. In other words, for weaker telemetry signals, the data rate is lowered in order to yield an acceptable energy per bit level E_b .

Assuming the data rate as been appropriately configured at the transmitter to ensure an acceptable constant value of E_b , it follows that the input signal power is given by $P_s = K \mathcal{R}_b$, where K is some constant value. In other words, the input signal power to the filter-decimate system will be proportionally lower for lower data rates. By using the decimation filter scaling rule given in Equation (2), we ensure that the *energy* of $H_k(z)$ is the same for all admissible values of k. This will result in amplifying the input signal power in such a way that the output signal power is constant for all power-of-two data rate

decimation factors while preserving the ambient noise psd level at N_0 . In essence, the scaling rule given in Equation (2) ensures that the signal level at the output of the filter-decimate system is (to within a factor of 2 to account for fine decimation factors) the same for all coarse power-of-two decimation factors, which is important for proper processing of the telemetry signal subsequently in the demodulator.

B. High-Rate Receiver Core

From Figure 1, it can be seen that the high-rate receiver core FPGA can accept input samples from either the input FPGA, which correspond to the 8-bit ADC digital IF signal sampled at 1.28 GHz, or the filter-decimate FPGA. The front-end of the receiver core includes coarse decimation by 2:1 and 4:1 followed by a fine interpolator which can accommodate a continuous range of decimation factors from 1:1 to 2:1. These operations can be applied to either set of input signals (i.e., the input FPGA or the filter-decimate FPGA). When applied to the input FPGA data samples, this front-end allows the accommodation of a continuum of decimation factors in the range from 8:1 to 1:1 (which corresponds to data rates from 40 MBd to 320 MBd). It should be noted that the baseband mixer used in the receiver core front-end is open-loop but not predict-driven, and so carrier frequency tracking for these higher data rates must be done entirely closed-loop in the demodulator.

After the fine interpolation stage in Figure 1, the resultant signal is scaled and can then be further downsampled via the integrate & dump system [2] and sent to the software demodulator, or input to the 4 sample/symbol hardware demodulator core. We now proceed to highlight two noteworthy aspects of the high-rate receiver core, namely, the fine interpolator system and the 4 sample/symbol demodulator core.

1. Fine Interpolator System

Suppose the overall decimation factor desired is \mathcal{D} . Here, we decompose \mathcal{D} into the product of *coarse* and *fine* decimation factors as follows:

$$\mathcal{D} = \mathcal{D}_C \mathcal{D}_F$$
, where $\mathcal{D}_C = 2^{\lfloor \log_2 \mathcal{D} \rfloor}$ and $\mathcal{D}_F = 2^{(\log_2 \mathcal{D}) \mod 1}$ (3)

In Equation (3), \mathcal{D}_C denotes the *coarse decimation factor* which is an integer power-of-two, whereas \mathcal{D}_F denotes the *fine decimation factor* which satisfies $1 \leq \mathcal{D}_F < 2$. For the RWGR hardware system, coarse decimation by a factor of \mathcal{D}_C is achieved through a combination of the filter-decimate system and/or the 2 : 1 and 4 : 1 decimation rates present in the front-end of the receiver core FPGA.

Fine decimation by a factor of \mathcal{D}_F , on the other hand, is achieved through the use of a fine interpolator system [6] contained in the receiver core. For the RWGR, a *linear* fine interpolator was used as shown in Figure 4. Here, fine decimation is carried out efficiently using a *Farrow structure* [6] for the interpolator.

The system shown in Figure 4 operates as follows. For every desired output sample y[n],



fine decimation factor - \mathcal{D}_F

Figure 4. Receiver core fine interpolator system block diagram.

the output time index n is first mapped to a quotient q and a remainder r. Specifically, q and r represent, respectively, the quotient and remainder of the decimated input time index $\mathcal{D}_F n$ when divided by unity. In other words, q and r are the integer and fractional parts of the number $\mathcal{D}_F n$, respectively. From Figure 4, it is clear that we have the following:

$$\mathcal{D}_F n = q + r$$
, where $q = \lfloor \mathcal{D}_F n \rfloor$ and $r = (\mathcal{D}_F n) \mod 1$ (4)

Here, q from Equation (4) is used to select data from the input stream x[m]. Specifically, q is used as a buffer offset parameter or pointer to input data samples of x[m] that are close to the desired decimated input time index $\mathcal{D}_F n$. Meanwhile, r is used as a weighting parameter to fine tune the data samples of x[m] near $\mathcal{D}_F n$ to the exact desired value. For a linear interpolation of the samples, the output sample y[n] is calculated as follows as shown in Figure 4:

$$y[n] = x[q] + r\left(x[q+1] - x[q]\right) = (1-r)x[q] + rx[q+1]$$
(5)

Intuitively, y[n] from Equation (5) is generated by constructing a linear fit between the closest samples of x[m] to the left and right of $m = \mathcal{D}_F n$, namely x[q] and x[q+1], respectively.

As the system of Figure 4 essentially decimates its input by a factor of \mathcal{D}_F , the input data stream x[m] should have been processed by an anti-aliasing filter to prevent aliasing at the output data stream y[n] [5]. Since the fine decimation factor \mathcal{D}_F satisfies $1 \leq \mathcal{D}_F < 2$, it is sufficient to use a *quarter-band* filter [5] (i.e., a low-pass filter with a cut-off frequency equal to a quarter of the input Nyquist rate [4]). Use of such a filter will essentially overly bandlimit the input data stream x[m] (especially for fine decimation factors close to 1), however, this will not be a problem here as this will amount to removing only out-of-band noise. In other words, since the telemetry signal of interest will always be oversampled by at least a factor of 4, the quarter band filter will not remove any of the desired signal spectral content.

For the RWGR, from Figure 1, it is seen that one of the possible inputs to the fine interpolator is the output of a filter. In accordance with the above analysis, this was



Figure 5. Block diagram of 4 sample/symbol demodulator core.

designed here to be a quarter-band anti-aliasing filter.

2. 4 sample/symbol Demodulator Core

An in-depth implementation block diagram of the 4 sample/symbol demodulator core is shown in Figure 5. Complex baseband samples from the receiver core front-end serve as the primary input of the demodulator. This input signal is then mixed by a complex input/complex output closed-loop NCO to remove residual Doppler frequency and carrier phase offset effects. Afterward, the resulting in-phase (I) and quadrature (Q) complex baseband arms [2] are each processed by a 17-tap reprogrammable linear phase [4] FIR matched filter [2].

The complex baseband output of the matched filter, which is operating at a clock rate of $4\mathcal{R}_d$, where \mathcal{R}_d denotes the data symbol rate, is sent to a closed-loop signal resampler to select the proper half symbols (operating at a clock rate of $2\mathcal{R}_d$) to use for the subsequent carrier phase/symbol timing tracking loops. These half symbols are placed in a first in, first out (FIFO) buffer [7] and, prior to sending them to the tracking loops, the I & Q half symbols are either sent directly or staggered depending on whether QPSK or OQPSK is the selected constellation type, respectively. The appropriate half symbols are then each sent to the carrier phase/symbol tracking loops. In addition, the half symbols are decimated by 2 (yielding samples at the data rate \mathcal{R}_d) to provide 16-bit soft symbols at the output. These soft symbols can either be stored in a random access memory (RAM) buffer [7] or output to a test port for further processing by a frame synchronizer and forward error correction (FEC) [2] decoder.

From among the various features of the 4 sample/symbol demodulator core, we will elaborate here on the signal resampler and the digitally implemented carrier phase/symbol timing tracking loops.

Signal Resampler A block diagram of the signal resampler used in the RWGR 4 sample/symbol demodulator core is shown in Figure 6. Here, the I & Q outputs of the



Figure 6. Signal resampler implementation block diagram.

matched filter (which are clocked at a rate of $4\mathcal{R}_d$) are upsampled [5] by a factor of 4 to provide a timing resolution of 1/16-th of a symbol. To suppress the presence of images inherent to the upsampling process [5], the resultant signal is applied to an anti-imaging filter $h_{\rm LI}[n]$. As can be seen from the impulse response of $h_{\rm LI}[n]$ shown in Figure 6, the combined effect of the upsampler followed by the filter is a *linear interpolation* of the input data [5]. In other words, a linear fit is used to describe data points that lie in between consecutive matched filter output samples.

After the input matched filter samples have been linearly interpolated by a factor of 4, the estimate k of the symbol timing offset from the Gardner loop [8] (along with an optional offset value of k_0) is used to effectively select the appropriate matched filter output samples. Once proper advance/delay timing has been established, the output is decimated by a factor of 8 to provide a stream of half symbol data (operating at a clock rate of $2\mathcal{R}_d$).

Carrier Phase/Symbol Timing Tracking Loops The carrier phase and symbol timing tracking loops are implemented entirely digitally in the 4 sample/symbol demodulator core as shown in Figure 5. For each case, the loop is implemented as follows. An error metric intended to measure the deviation of the tracking loop estimate from its desired value is first calculated. This error is then filtered by a loop filter to help mitigate against the effects of additive noise present in the system. The output of this loop filter serves as the estimate of the quantity to be tracked and is used to drive the complex NCO and symbol resampler for the carrier phase and symbol timing loops, respectively.

For each loop, the error metric used is derived via a computational simplification of the *maximum likelihood* (ML) estimate [2] of the quantity to be estimated. Specifically, for the carrier phase offset, the error metric used is the polarity-type *Costas* error function [8], which is derived from a high SNR approximation of the ML estimate of the carrier phase. Similarly, for the symbol timing offset, the error metric used is the *Gardner* error function [8], which is derived from the ML estimate of the symbol timing.

Explicit expressions for the Costas and Gardner error functions used in the 4 sample/symbol demodulator core are given as follows. Let I[n] and Q[n] denote the I & Q data sequences at the output of the signal resampler from Figure 5 and 6. Note that both I[n] and Q[n] are half symbol streams (operating at a clock rate of $2\mathcal{R}_d$). If $\epsilon_{\rm C}[n]$ and $\epsilon_{G}[n]$ denote the Costas and Gardner error sequences used here, respectively, then we have the following [8]:

$$\epsilon_{\rm C}[n] = \begin{cases} Q[n+1] \operatorname{sgn}(I[n+1]) - I[n+1] \operatorname{sgn}(Q[n+1]) \\ + Q[n+3] \operatorname{sgn}(I[n+3]) - I[n+3] \operatorname{sgn}(Q[n+3]) \end{cases}, \text{ for QPSK} \\ Q[n] \operatorname{sgn}(I[n]) - I[n+1] \operatorname{sgn}(Q[n+1]) \\ + Q[n+2] \operatorname{sgn}(I[n+2]) - I[n+3] \operatorname{sgn}(Q[n+3]) \end{cases}, \text{ for OQPSK} \end{cases}$$

$$\epsilon_{\rm G}[n] = \begin{cases} (I[n+1] - I[n-1]) I[n] \\ + (Q[n+1] - Q[n-1]) Q[n] \\ + (Q[n+3] - I[n+1]) I[n+2] \\ + (Q[n+3] - Q[n+1]) Q[n+2] \\ (I[n] - I[n-2]) I[n-1] \\ + (Q[n+1] - Q[n-1]) Q[n] \\ + (I[n+2] - I[n]) I[n+1] \\ + (Q[n+3] - Q[n+1]) Q[n] \end{cases}, \text{ for OQPSK} \end{cases}$$

$$(7)$$

Here, the function sgn(x) used in Equation (6) denotes the *signum* function, which is defined as follows:

$$\operatorname{sgn}(x) \triangleq \begin{cases} -1, & x < 0\\ 1, & x \ge 0 \end{cases}$$

From Equation (6) and Equation (7), it is clear that the Costas and Gardner error metrics change depending on whether QPSK or OQPSK is used. This is done here to account for the fact that the I & Q arms in OQPSK are staggered by one half of a symbol [2]. One effect of this is better performance for carrier phase tracking for OQPSK compared to QPSK [2], since phase shifts due to changing data patterns are limited to 90° for OQPSK but are 180° for QPSK [2].

Assuming acquisition has been properly established for each loop, which will be the case here for both Costas and Gardner derived tracking loops [8], then the error metric in each case will be relatively small compared to its transient levels during acquisition. In this case, the overall tracking loop can be approximately represented by a linearized model. This is shown in Figure 7 for a general tracking loop.

Here, x[n] denotes the quantity to be estimated and tracked (i.e., either the carrier phase offset or symbol timing offset), whereas $\hat{x}[n]$ denotes the loop estimate of x[n]. The quantity $\epsilon[n] \triangleq x[n] - \hat{x}[n]$ denotes the *error metric*, which would be $\epsilon_{\rm C}[n]$ from Equation (6) for the Costas loop and $\epsilon_{\rm G}[n]$ from Equation (7) for the Gardner loop.

From Figure 7, it can be seen that the error metric $\epsilon[n]$ gets scaled by the loop gain A,



Figure 7. Linearized tracking loop model.

filtered by the *loop filter* F(z), and is subjected to a *loop delay* of L samples to produce the loop estimate $\hat{x}[n]$. An *open-loop* description of the model from Figure 7 can be expressed as follows [4]:

$$\widehat{x}[n] = \{A\epsilon[n-L]\} * f[n] \tag{8}$$

Here, * denotes the convolution operator and f[n] denotes the impulse response of F(z)[4]. From Equation (8), it is clear that while in tracking mode, the loop estimate $\hat{x}[n]$ is obtained by filtering a scaled, delayed version of the loop error $\epsilon[n]$ by the loop filter F(z).

By exploiting the relation $\epsilon[n] = x[n] - \hat{x}[n]$, we can obtain a *closed-loop* description of the model from Figure 7. To that end, let X(z) and $\hat{X}(z)$ denote the z-transforms [4] of x[n] and $\hat{x}[n]$, respectively, and let $H(z) \triangleq \frac{\hat{X}(z)}{X(z)}$ denote the *loop transfer function* [8]. Then, from Equation (8), we have the following:

$$H(z) = \frac{Az^{-L}F(z)}{1 + Az^{-L}F(z)}$$
(9)

The loop transfer function H(z) from Equation (9) is typically low-pass [8] and dictates the amount of input noise which can be suppressed and the level of dynamics that can be tracked by the loop. As may be expected, there is a trade-off between these two goals. If H(z) is narrowband, the input noise is suppressed at the expense of the tracking ability of the loop. Similarly, if H(z) is wideband, then the loop can track a desired parameter with a higher degree of varying dynamics at the expense of increased noise power within the loop. In essence, the loop transfer function H(z) should be narrowband for noisy, low dynamic environments and should be wideband for low noise, high dynamic environments [8].

Quantitatively, the noise suppression/tracking abilities of the loop can be measured by computing the normalized loop bandwidth $B_{\ell}T_u$, where B_{ℓ} denotes the underlying analog loop bandwidth and T_u denotes the update time of the loop [8] (which will always be given by $T_u = \frac{2}{\mathcal{R}_d}$ here). The normalized loop bandwidth product $B_{\ell}T_u$ is given in terms of the loop transfer function H(z) as shown below [8]:

$$B_{\ell}T_{u} = \frac{1}{2} \int_{-\frac{1}{2}}^{\frac{1}{2}} \left| H\left(e^{j2\pi f}\right) \right|^{2} df$$
(10)

For a given loop and given set of input operating conditions, the loop gain A and loop

delay L are fixed, and so the only degree of freedom available for changing H(z) (and hence $B_{\ell}T_u$ from Equation (10)) is to alter the loop filter F(z) from Equation (9). From Figure 7, it can be seen that the loop filter F(z) here is a second-order filter with the following transfer function:

$$F(z) = \frac{\alpha}{1 - z^{-1}} + \frac{\beta}{(1 - z^{-1})^2} = \frac{\alpha \left(1 - z^{-1}\right) + \beta}{\left(1 - z^{-1}\right)^2}$$
(11)

From Equation (9) and Equation (11), it can be seen that the linearized loop characteristics here are solely a function of the quantities A, L, α , and β . These quantities are different for the Costas and Gardner loops. As such, let $A_{\rm C}$, $L_{\rm C}$, $\alpha_{\rm C}$, and $\beta_{\rm C}$ denote the quantities characterizing the Costas loop and $A_{\rm G}$, $L_{\rm G}$, $\alpha_{\rm G}$, and $\beta_{\rm G}$ denote those characterizing the Gardner loop. Similarly, let $(B_{\ell}T_u)_{\rm C}$ and $(B_{\ell}T_u)_{\rm G}$ denote the normalized loop bandwidths of the Costas and Gardner loops, respectively.

For the tracking loops present in the RWGR 4 sample/symbol demodulator core, the loop gains $A_{\rm C}$ and $A_{\rm G}$ will depend upon the input signal level and must be assessed on a case by case basis. However, from the implementation of the demodulator core, it is known that we have $L_{\rm C} = 5$ for the Costas loop and $L_{\rm G} = 7$ for the Gardner loop. By default, we also have $\alpha_{\rm C} = -1 \times 10^4$ and $\beta_{\rm C} = 0$ for the Costas loop and $\alpha_{\rm G} = -1 \times 10^4$ and $\beta_{\rm G} = 0$ for the Gardner loop. From these values, the Costas and Gardner loop transfer functions need to be evaluated using Equation (9) to obtain the normalized loop bandwidths $(B_{\ell}T_u)_{\rm C}$ and $(B_{\ell}T_u)_{\rm G}$, respectively, using Equation (10).

In general, for each tracking loop, increases in either α or β or both will result in an increased normalized loop bandwidth $B_{\ell}T_u$. This is in line with intuition, as larger values of α and β will imply a larger dynamic range at the output of the loop filter F(z). Approximate expressions relating α and β to $B_{\ell}T_u$ are provided in [8, 9].

We now proceed to present hardware performance results for the RWGR for a variety of input test scenarios.

III. Hardware Performance Results

To test the RWGR hardware receiver, an arbitrary waveform generator (AWG) was used to convert digital baseband telemetry to an analog IF format to be received by the RWGR. Additive white Gaussian noise (AWGN) was added to this analog IF waveform and the resultant noisy IF signal was sent to the ADC at the front-end of the RWGR for sampling.

A. Noiseless Soft Decision Outputs

To qualitatively gauge the ability of the RWGR to properly demodulate telemetry and track both carrier phase and symbol timing offsets, we opted to show constellation density plots of noiseless soft decision outputs. These are two-dimensional logarithmic histogram plots of the output I & Q soft symbols. In addition to considering QPSK and OQPSK, for

which the RWGR was primarily configured, we also opted to consider bandwidth efficient modulation types such as GMSK and 16-QAM. For all of the results presented here, a data symbol rate of 160 MBd was used.

In Figure 8, we have plotted the noiseless output constellation density plots for a variety of pulse shaped waveforms. Specifically, square-root raised cosine (SRRC) [2] pulse shapes with different roll-off factors ρ were considered in addition to rectangular shaped non-return to zero (NRZ) pulses. In Figure 8(a) and (b), SRRC pulse shapes with roll-off factors of 0.35 and 0.5 were considered, respectively, whereas in Figure 8(c), an NRZ pulse shape was used.

As can be seen, there is more dispersion for the 0.35 roll-off SRRC constellation than for the 0.5 roll-off case. The reason for this is that the underlying impulse response of the 0.35 roll-off SRRC pulse decays more slowly than that corresponding to the 0.5 roll-off case [2]. As such, there is more residual intersymbol interference (ISI) [2] for $\rho = 0.35$ than for $\rho = 0.5$ on account of the fact that the matched filters used in the RWGR are FIR [4]. Specifically, the 17-tap FIR matched filter used in the 4 sample/symbol demodulator core spans four symbol intervals of the underlying impulse response of the pulse shaping filter. To see this, note that if p(t) denotes the transmit pulse shaping filter, then the 17-tap FIR matched filter is given by $p_{\rm MF}[n] = p^* \left(-\frac{nT_d}{4}\right)$ for $-8 \le n \le 8$, where T_d denotes the data symbol interval. The FIR matched filter thus spans a time interval of $-2T_d \le t \le 2T_d$, which corresponds to four symbol intervals (two to the left of the center and two to the right).

From Figure 8(c), it can be seen that the NRZ pulse shape yielded the most dispersion of the output constellations considered. The reason for this is that even though the original transmit pulse shape $p_{\text{NRZ}}(t)$ used for NRZ is rectangular and finite in duration, the effective transmit pulse shape seen by the receiver is approximately $q_{\text{NRZ}}(t) = p_{\text{NRZ}}(t) * \operatorname{sinc}\left(\frac{4t}{T_d}\right)$ on account of the anti-aliasing analog low-pass filtering used prior to sampling the analog IF waveform [4]. Here, $\operatorname{sinc}(x)$ is the *normalized sinc function* defined as $\operatorname{sinc}(x) \triangleq \frac{\sin(\pi x)}{\pi x}$. Due to the anti-aliasing filter, the effective transmit pulse shape $q_{\text{NRZ}}(t)$ seen is infinite in length and decays very slowly on account of the *Gibbs phenomenon* [4]. As a result, the residual ISI present for NRZ will be greater than for either SRRC case considered here. This residual ISI manifests itself as increased dispersion of the output constellation, as seen in Figure 8.

In Figure 9, we plotted the noiseless output constellation density plots for GMSK for two different normalized bandwidths [3] (BT = 0.25 for Figure 9(a) and BT = 0.5 for Figure 9(b)). Here, the receiver matched filter used consisted of samples of the first amplitude modulated pulse (AMP) component [10] of the constant envelope GMSK waveform and the RWGR was configured for OQPSK. As can be seen, there was noticeable dispersion for both cases. The reason for this is that GMSK is a constant envelope waveform with inherent memory effects [3]. As a result, symbol-by-symbol detection is not optimal [3], as evidenced by the visible dispersion for both cases.



Figure 8. Noiseless constellation density plots for QPSK using a variety of pulse shaping filters: (a) SRRC, $\rho = 0.35$, (b) SRRC, $\rho = 0.5$, (c) NRZ.



Figure 9. Noiseless constellation density plots for GMSK for a normalized bandwidths of (a) BT = 0.25 and (b) BT = 0.5.

From Figure 9, it can be seen that there was more dispersion for the case of BT = 0.25[Figure 9(a)] than for BT = 0.5 [Figure 9(b)]. The reason for this is primarily that the first AMP component for BT = 0.25 is less dominant over the other components than for BT = 0.5 [3]. As a result, there is effectively more residual ISI for BT = 0.25 than for BT = 0.5 when a single matched filter is used for symbol-by-symbol detection. As will be shown in Section III.B.3, this increased dispersion manifests itself as a degradation in BER.

Finally, in Figure 10, we have plotted the noiseless output constellation density plot for 16-QAM using an SRRC pulse shaping filter with roll-off $\rho = 0.35$. As can be seen, both carrier phase and symbol timing offsets were tracked for this case, even though the RWGR was specifically designed for QPSK/OQPSK. This brings to light the possibility of using the RWGR to receive higher order modulation types.



Figure 10. Noiseless constellation density plot for $16\mbox{-QAM}$ using an SRRC pulse shaping filter with roll-off $\rho=0.35.$

B. Uncoded BER Results

We now proceed to present uncoded BER hardware performance results for the RWGR. In addition to presenting high data rate results in Section III.B.1, which include simulations which only require the high-rate receiver core FPGA, we also present results for various data rates in Section III.B.2, which include simulations that require both the front-end filter-decimate FPGA and the receiver core FPGA. Furthermore, we also present results for demodulation of GMSK in Section III.B.3.

Unless specified otherwise, all BER results were carried out for QPSK using an SRRC pulse shape with a roll-off of $\rho = 0.35$. Also, all BER results were plotted alongside the ideal uncoded BER [2]. For QPSK, this is given by the following expression:

$$P_b = Q\left(\sqrt{\frac{2E_b}{N_0}}\right) \tag{12}$$

Here, P_b denotes the bit-error probability, E_b/N_0 is the bit SNR, and Q(x) is the Marcum Q-function [2].

1. High Data Rate Results

A plot of the uncoded BER hardware results for QPSK at the maximal symbol rate of 320 MBd is shown in Figure 11. As can be seen, the implementation losses can be somewhat large for lower BERs. Specifically, it can be seen that for a BER of 2×10^{-6} , the implementation loss is about 1.75 dB.

Experimentally, it was verified that one of the primary causes of this large implementation loss was that the test equipment used to generate the IF waveform input to the RWGR limited the bandwidth of the transmitted signal. Specifically, the arbitrary waveform generator (AWG) used to generate the IF input signal non-negligibly low-pass filtered the transmit waveform for symbol rates above ~ 240 MBd. This low-pass filtering significantly



Figure 11. Uncoded BER results for QPSK at the maximum symbol rate 320 MBd (corresponding to 640 Mbps).

increased the ISI of the received signal and resulted in degraded performance for demodulation at the receiver end.

For all symbol rates below 240 MBd that were tested here, it was found that implementation losses were less than 1 dB and typically ~ 0.5 dB. This can be seen, for example, for the BER results shown in Figure 12 for QPSK and OQPSK at a symbol rate of 160 MBd. From Figure 12, it is indeed seen that the implementation losses in this case were around 0.5 dB. As expected, it can be seen that the performance yielded for both QPSK and OQPSK were about the same here.

2. Variable Data Rate Results

In Figure 13, we have plotted the uncoded BER hardware results for a variety of input data rates. For several of these rates, the filter-decimate front-end FPGA was utilized in addition to the fine interpolator system of the receiver core FPGA. As can be seen, the empirical BER measured was very close to the ideal BER from Equation (12) for all rates considered here. Implementation losses for all rates considered were found to be on the order of 0.5 dB.

To highlight the advanced acquisition/tracking capabilities and low implementation losses of the RWGR, zoomed in versions of the results from Figure 13 are shown in Figure 14 for



Figure 12. Uncoded BER results for QPSK and OQPSK at a symbol rate of 160 MBd (corresponding to 320 Mbps).



Figure 13. Uncoded BER results for QPSK at several data rates.



Figure 14. Close-up of Figure 13 for (a) the low bit SNR regime and (b) the high bit SNR regime.

(a) the low bit SNR and (b) the high bit SNR regimes. Specifically, the exceptional tracking performance of the RWGR can be seen in Figure 14(a), where it can be seen that acquisition and tracking is feasible for very low bit SNR (less than -10 dB). This tracking ability is especially important for deep space applications which typically operate at low bit SNRs (can be as low as -5 dB bit SNR for advanced error correcting codes such as LDPC).

In Figure 14(b), the implementation losses at high bit SNR are on the order of 0.5 dB and indicate that the receiver is operating close to its theoretically optimal value. The implementation losses here are a combination of losses due to quantization internal to the receiver and residual ISI due to the finite length matched filters used at the receiver. From Figure 14(b), it is seen that the net effects of these losses is minimal.

3. GMSK Demodulation Results

To evaluate the uncoded BER performance of GMSK in hardware, for all cases considered here, the first AMP component [10] of the GMSK waveform under consideration was used as the matched filter. In Figure 15, we have plotted the BER obtained for GMSK at a symbol rate of 160 MBd. Here, we considered normalized bandwidths of BT = 0.25 and BT = 0.5.

From Figure 15, it can be seen that the implementation losses at a BER of 10^{-5} were around 1.5 dB for BT = 0.25 and around 0.5 dB for BT = 0.5. One of the reasons for the larger implementation loss for BT = 0.25 is that in this case, the first AMP component is not as dominant over the rest of the components as it is for BT = 0.5. As a result, there is more residual ISI for this case than for BT = 0.5 and hence larger implementation losses.

To elucidate the acquisition/tracking abilities and implementation losses for GMSK, zoomed in versions of the results from Figure 15 are shown in Figure 16 for (a) the low bit



Figure 15. Uncoded BER results for GMSK at a symbol rate of 160 MBd (corresponding to 320 Mbps).

SNR and (b) the high bit SNR regimes. From Figure 16(a), it can be seen that the RWGR exhibited exceptional tracking performance for low bit SNRs. Implementation losses in this case were very low and less than 0.5 dB for both BT = 0.25 and BT = 0.5. This suggests that effects due to noise are more pronounced for this region than residual ISI effects inherent to the GMSK waveform.

In Figure 16(b), we highlight the implementation losses for GMSK at high bit SNR. It can be seen that the losses at 10^{-5} are around 1.5 dB for BT = 0.25 and 0.5 dB for BT = 0.5. As mentioned above, this is primarily due to the fact that there is more residual ISI for BT = 0.25 than for BT = 0.5. Specifically, this is consistent with the GMSK constellation density plots shown in Figure 9.

This brings to light the fact that symbol-by-symbol demodulation of GMSK is suboptimal [2]. In order to obtain optimal performance, a Viterbi algorithm based trellis demodulation [2] would be required here in order to fully address the memory or ISI inherent to the GMSK waveform. Such demodulation however is highly computationally complex. In many cases, it is worthwhile accepting the increased implementation losses of a symbol-by-symbol based demodulation in order to preserve the simplicity of the receiver implementation.



Figure 16. Close-up of Figure 15 for (a) the low bit SNR regime and (b) the high bit SNR regime.

IV. Concluding Remarks

In addition to providing a hardware implementation description of the RWGR, several laboratory performance results were presented. As was shown, the RWGR was capable of demodulating a variety of telemetry waveform types (QPSK, OQPSK, GMSK, etc.) at several data rates. Furthermore, it was shown that for most cases, the implementation loss was on the order of 0.5 dB bit SNR. In addition, we also demonstrated carrier phase/symbol timing tracking for low bit SNR (< -5 dB) for all cases considered. This brings to light the advantages of the RWGR for deep space communications applications.

Future work consists of incorporating frame synchronizer & FEC decoder FPGAs to the RWGR soft symbol outputs. Once this has been accomplished, it will be necessary to characterize performance losses of the combined demodulation and decoding functions of the receiver through a series of laboratory hardware tests.

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